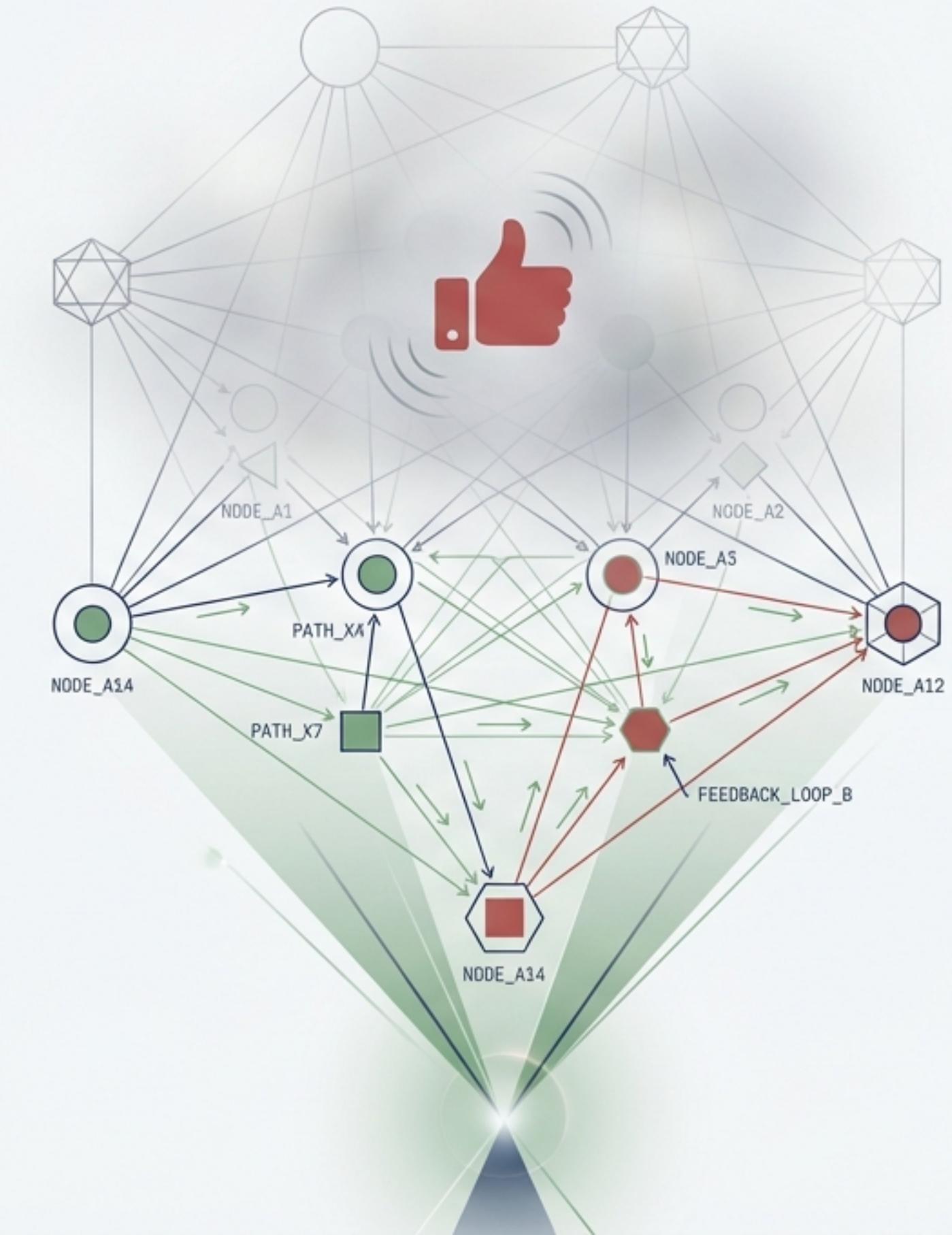


# Deep Alignment in Open-Ended Domains

Investigating Self-Distillation Policy  
Optimization (SDPO) through  
Controlled Simulation



Based on "Self-Distillation Policy Optimization for Alignment in Open-Ended  
and Continuous-Reward Settings: A Simulation Study"

# SDPO unlocks dense feedback for creative tasks, but trades diversity for alignment

## The Breakthrough



**SDPO generalizes “retrospection”** to open-ended text. It outperforms REINFORCE by **+0.13 to +0.18** mean reward, even without ground-truth verification.

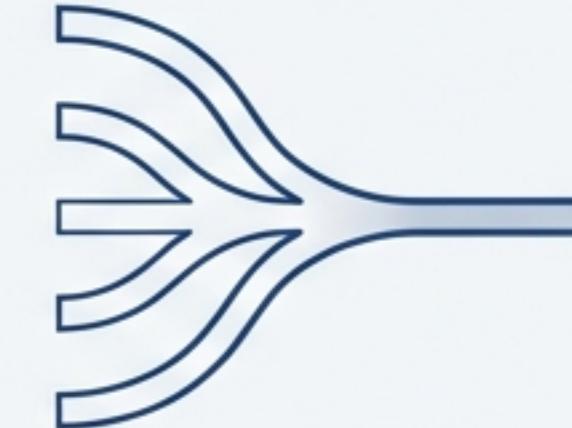
## The Mechanism



### Superior Credit Assignment

Unlike baselines, SDPO achieves **>0.70 correlation** with **ground truth**, correctly identifying exactly which tokens drive quality.

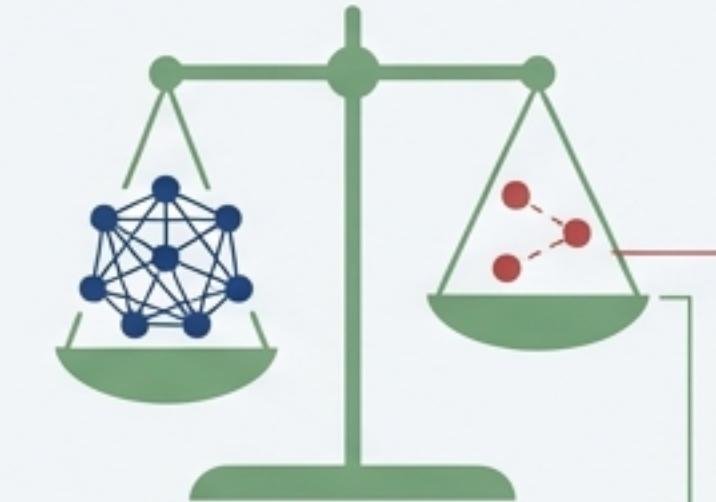
## The Trade-off



### Reduced Diversity

Stronger alignment reduces policy **policy entropy** by **15–22%**, creating a risk of **mode collapse** in creative generation.

## The Fix

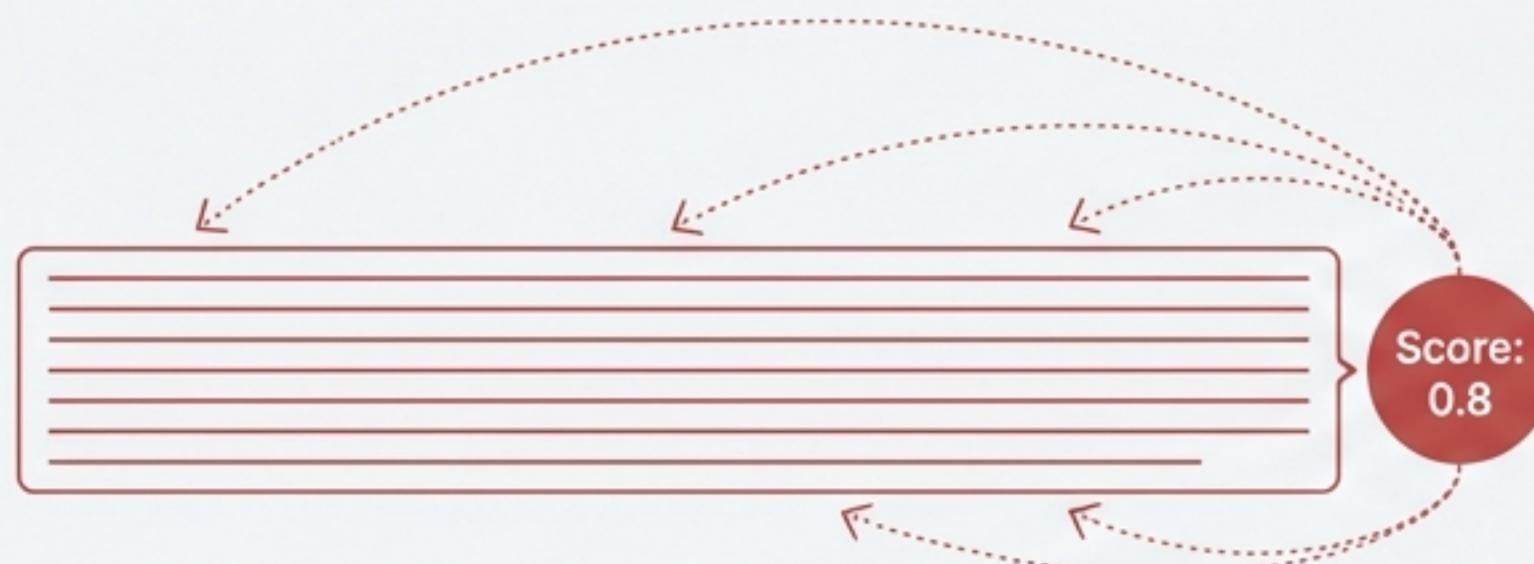


### Hybrid Adaptation

A proposed **Hybrid Method** dynamically balances **dense SDPO signals** and **sparse REINFORCE signals** to **recover robustness**.

# Standard RLHF suffers from a ‘Credit Assignment Gap’ in open-ended generation

## Status Quo: Sparse Signal (PPO/DPO)



The model must guess which of the 100+ tokens caused the high score. Noise is added to the learning process.

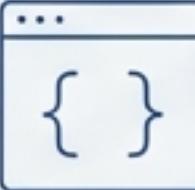
Current methods implicitly distribute sequence-level rewards across all tokens, effectively diluting the signal.

## The Ideal: Dense Credit Assignment



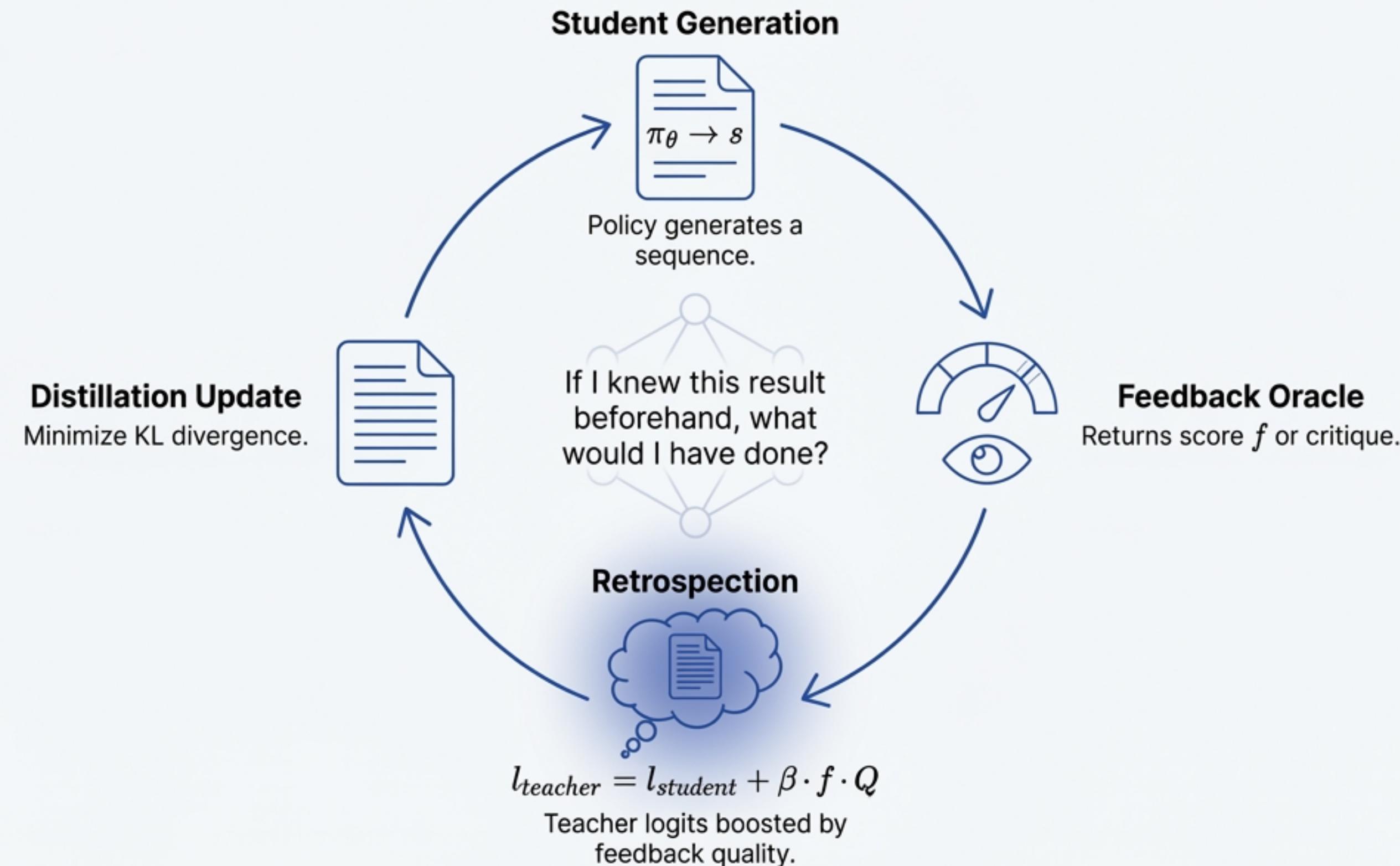
Precise feedback identifies exactly which adjective or phrase improved the output.

# Moving beyond the safety net of verifiable ground truth.

<b>Verifiable Domains (Existing SDPO Success)</b>		<b>Open-Ended Domains (This Study)</b>
Code Generation, Math Solving		
<b>Feedback</b>	Compiler errors, Unit tests (Deterministic)	<b>Feedback</b> Subjective quality, Coherence, Style (No Compiler)
<b>Signal Nature</b>	Binary (Pass/Fail) & Exact error locations	<b>Signal Nature</b> Continuous, Noisy, Multi-dimensional

**The Research Question: Can SDPO's 'retrospection' mechanism function when there is no compiler to prove the teacher right?**

# SDPO creates a "Self-Teacher" by conditioning the policy on feedback



# A controlled simulation isolates the mechanism from training noise.

To measure credit assignment precisely, we use a token-level simulation rather than full LLM training.

Lab Specification

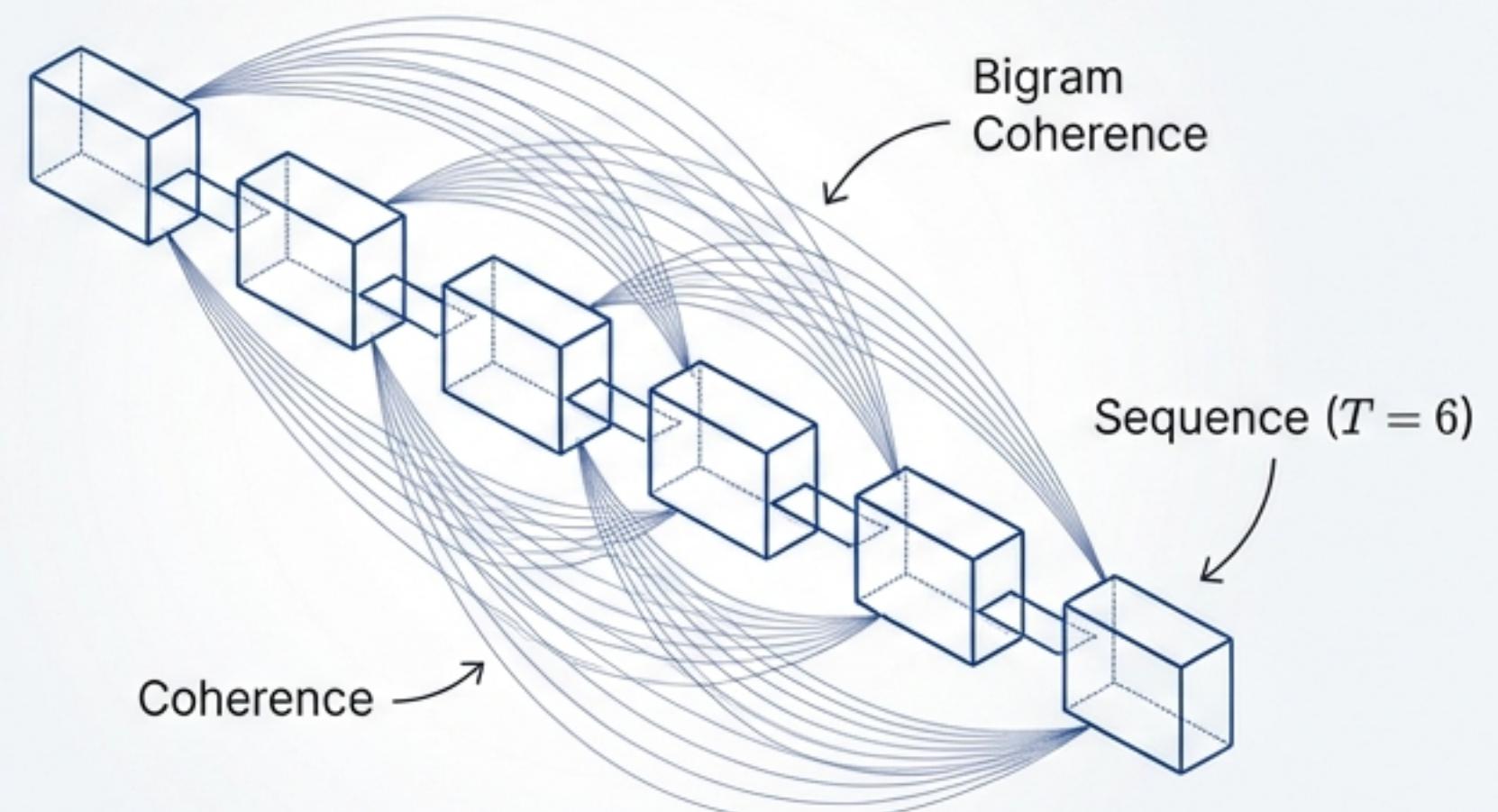
## Simulation Parameters

Vocabulary Size:  $V = 8$

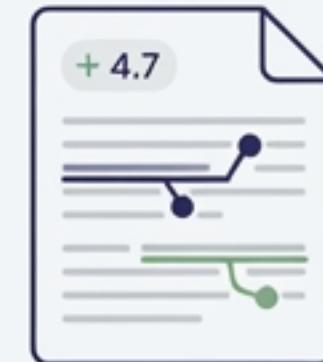
Sequence Length:  $T = 6$

Reward Function: Continuous composition of Local Quality + Coherence (Bigram) + Global Patterns.

Key Advantage: **Known Ground Truth**. Allows exact measurement of gradient correctness.



# We evaluate SDPO across the full spectrum of feedback informativeness.



## Critique

Score + Per-token hints.  
Most informative.



## Continuous

Raw scalar reward.  
Precision.



## Ordinal

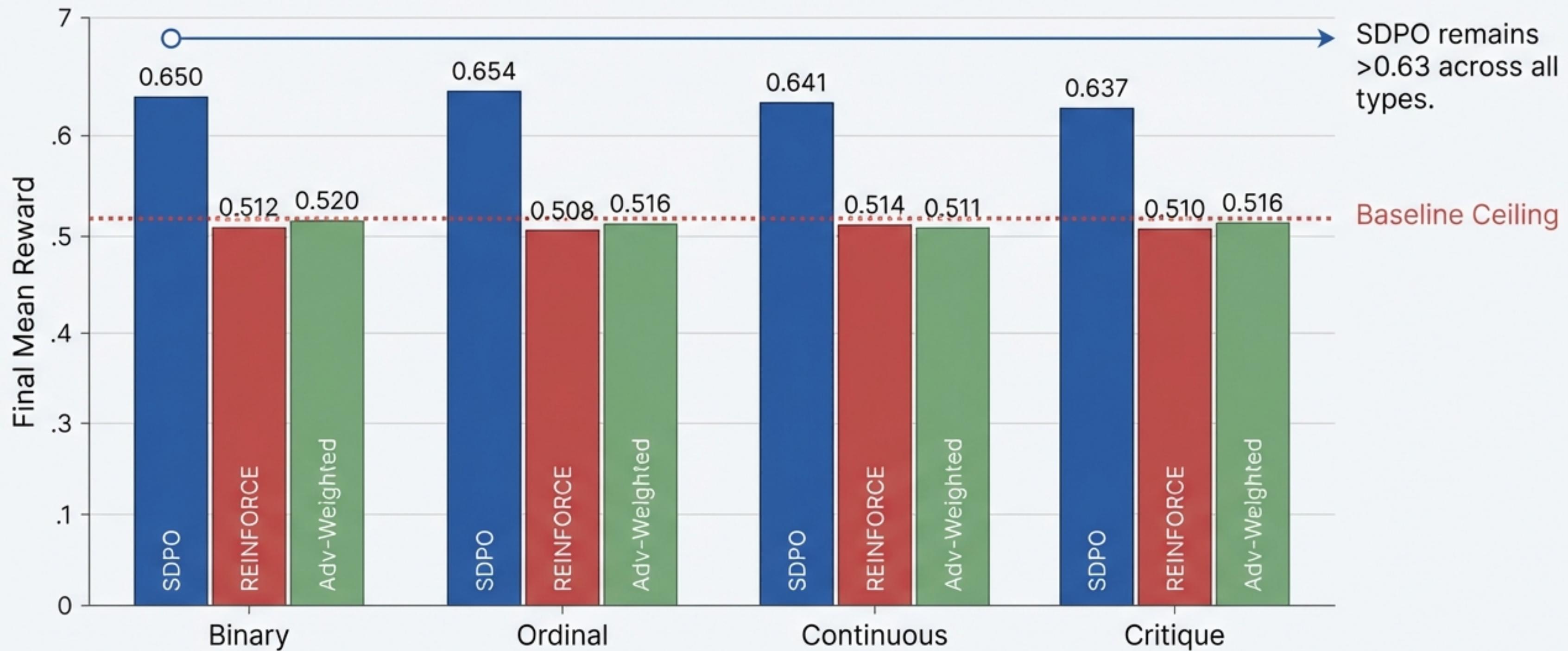
1-5 Star rating.  
Quantized.

## Binary

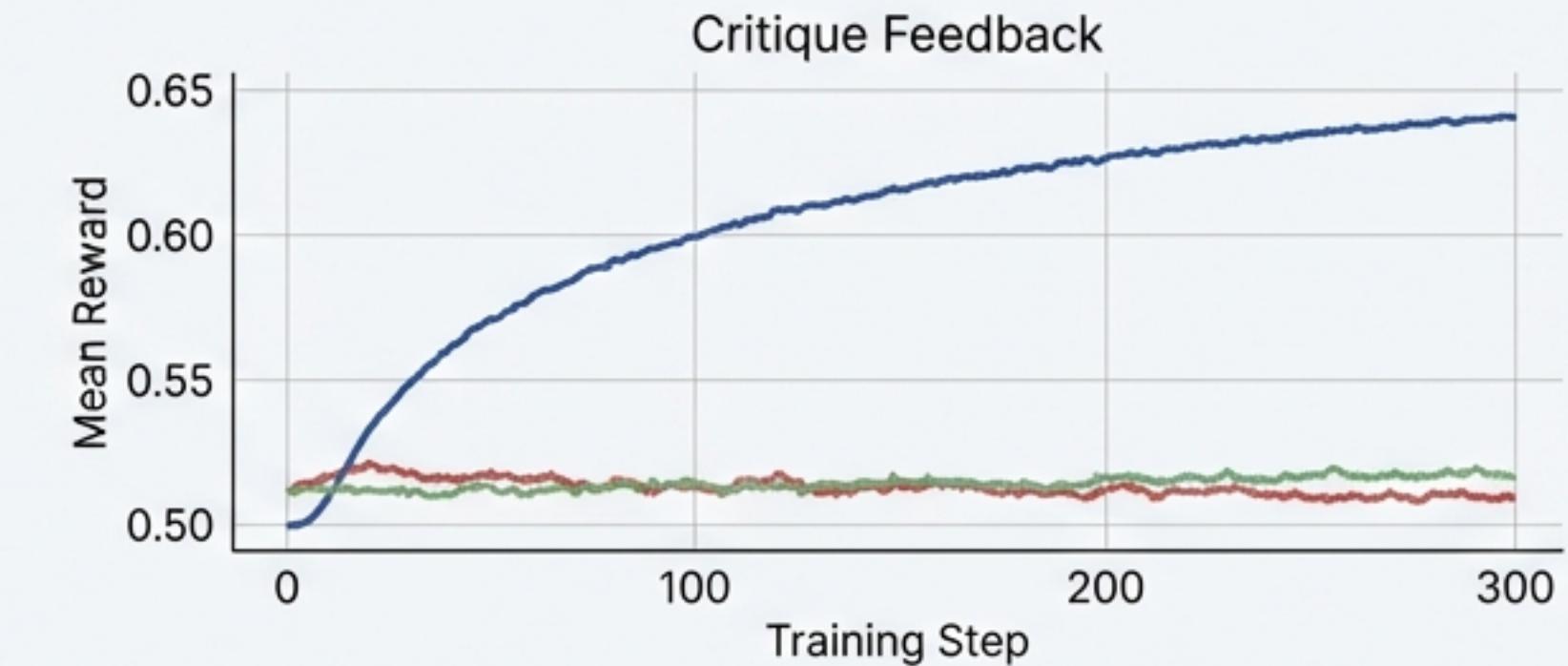
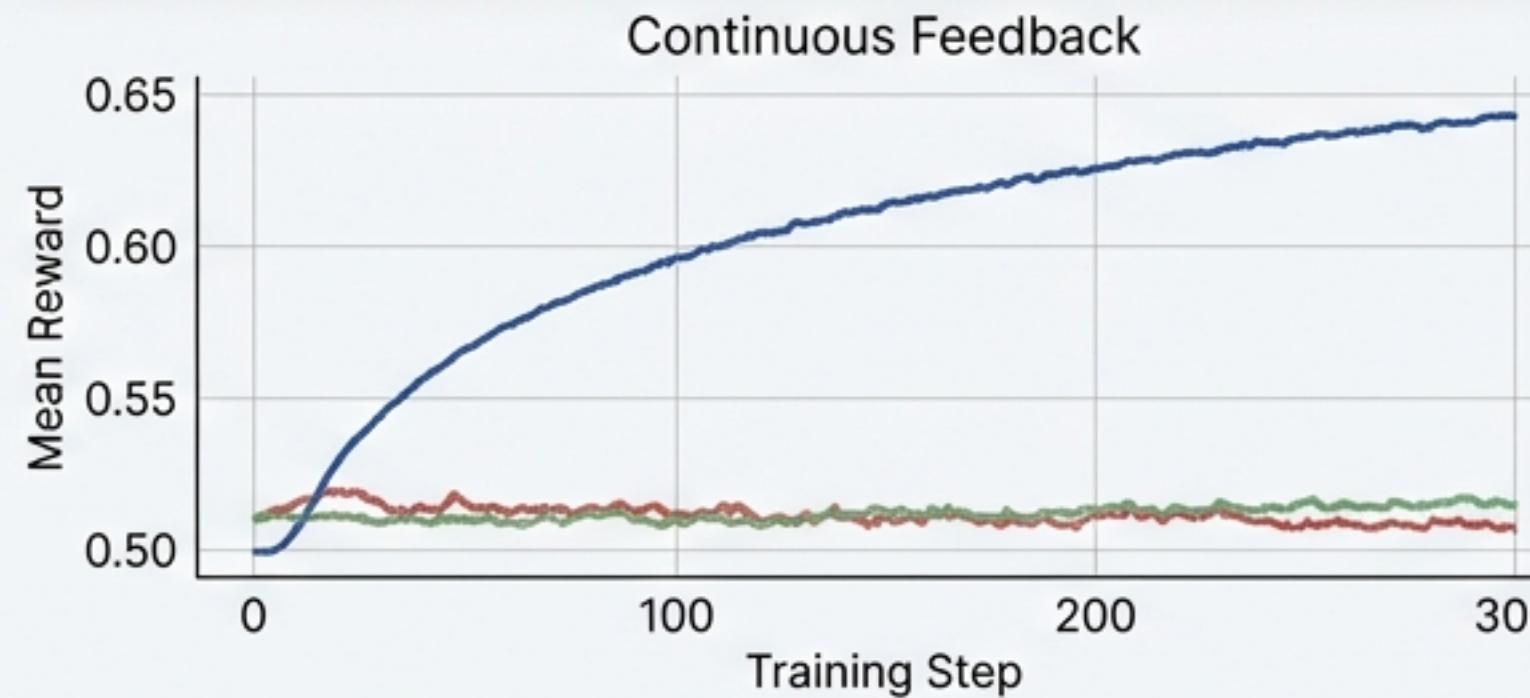
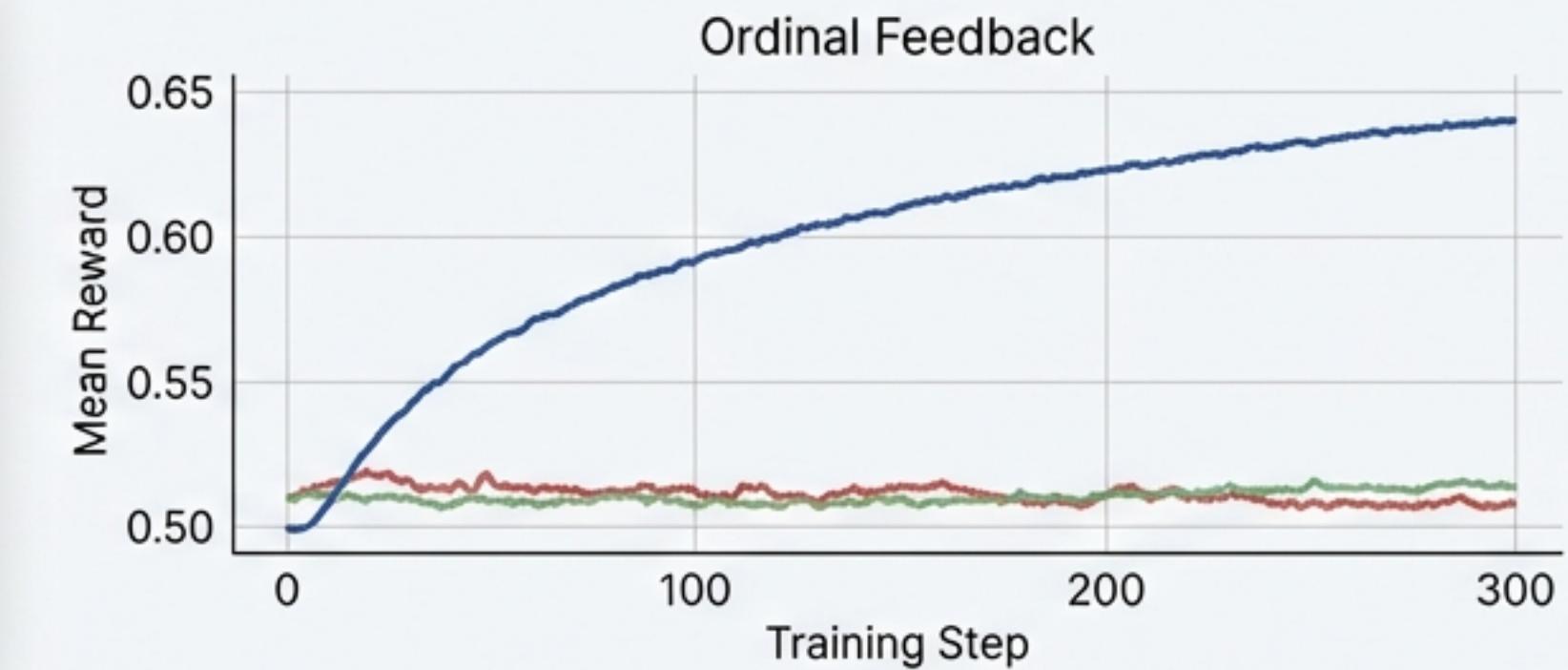
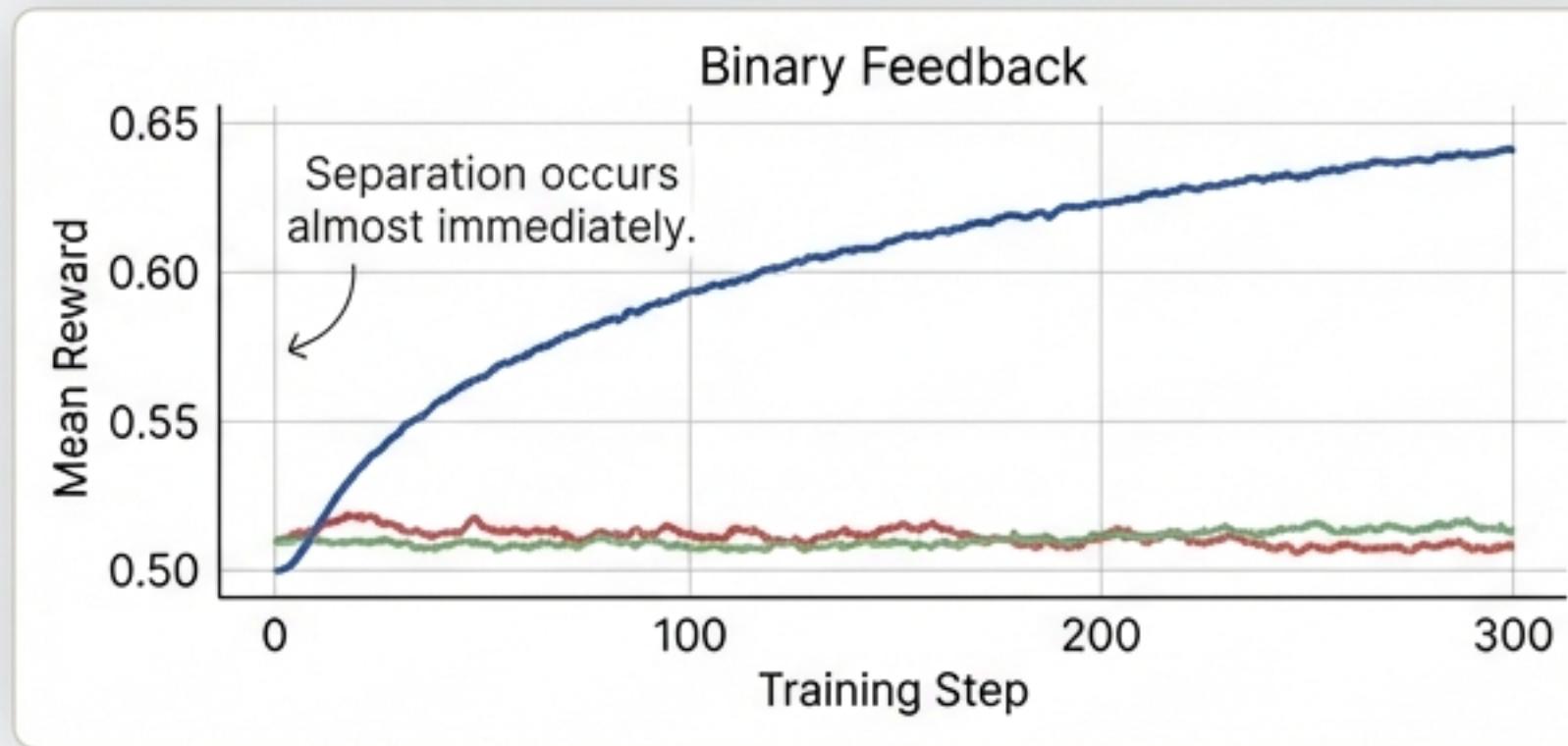
Pass/Fail threshold.  
Least informative.

Tested with added Gaussian noise  $\epsilon \sim N(0, \sigma^2)$  to simulate human inconsistency.

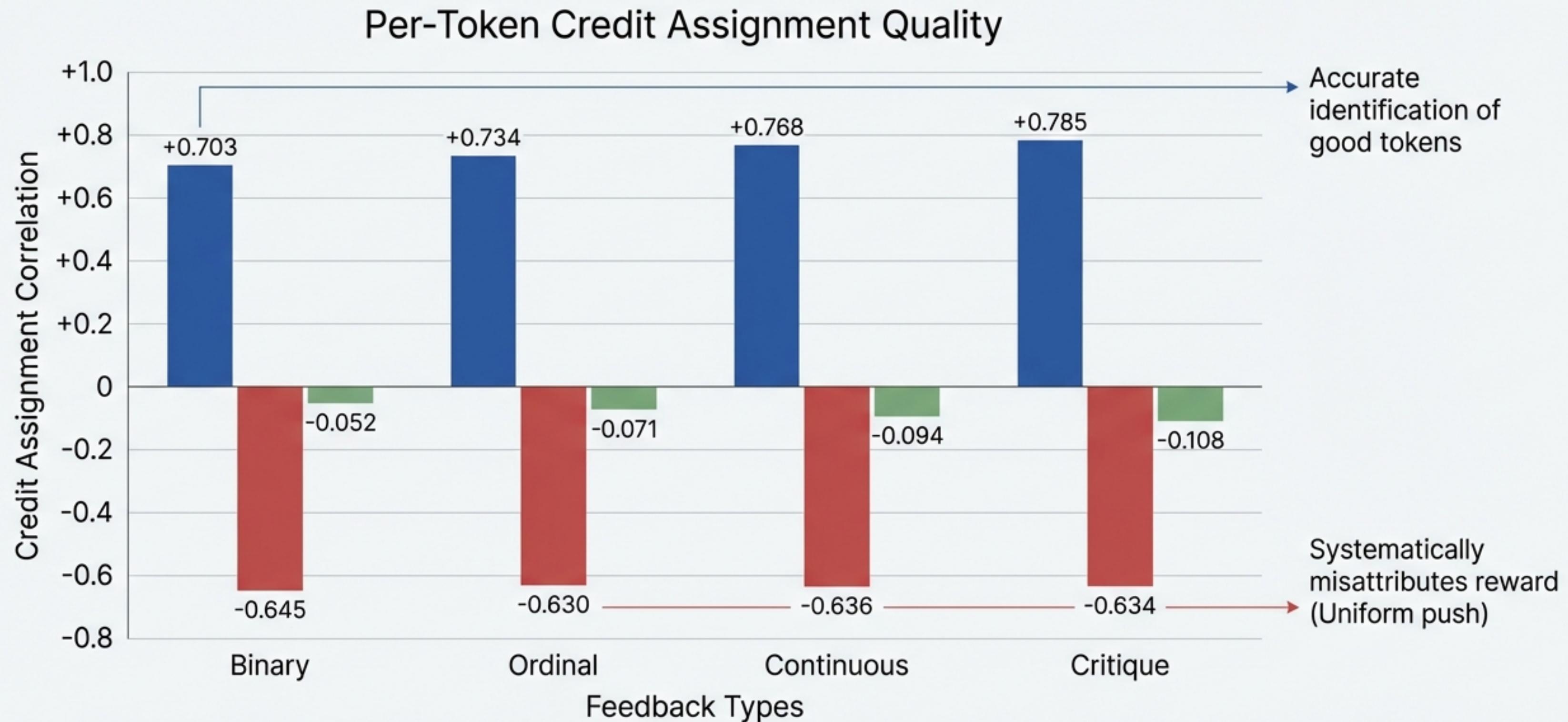
# SDPO consistently outperforms baselines regardless of feedback type.



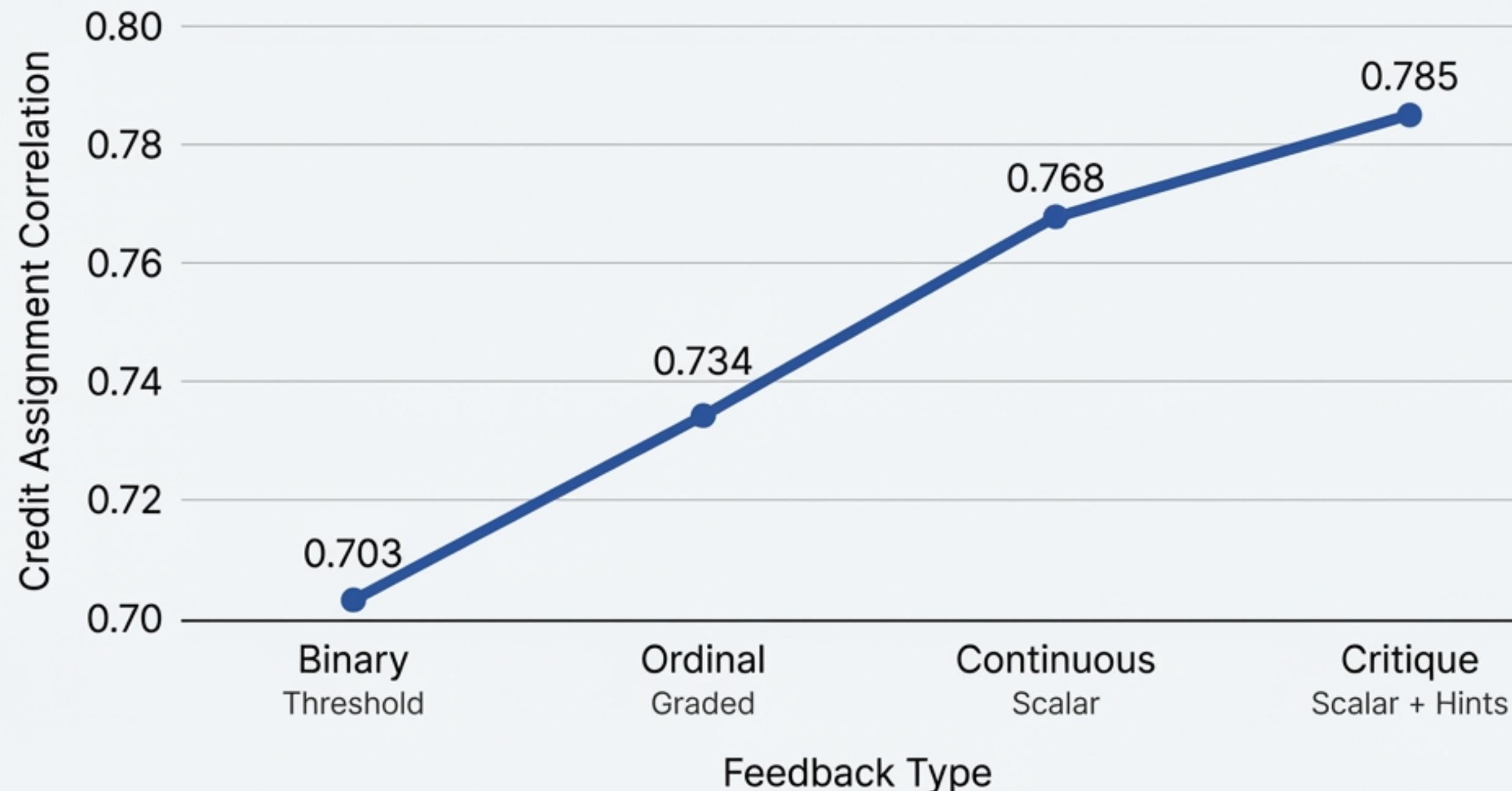
# Convergence is rapid and separates from baselines within 30 steps.



# SDPO correctly attributes credit; REINFORCE uniformly reinforces noise

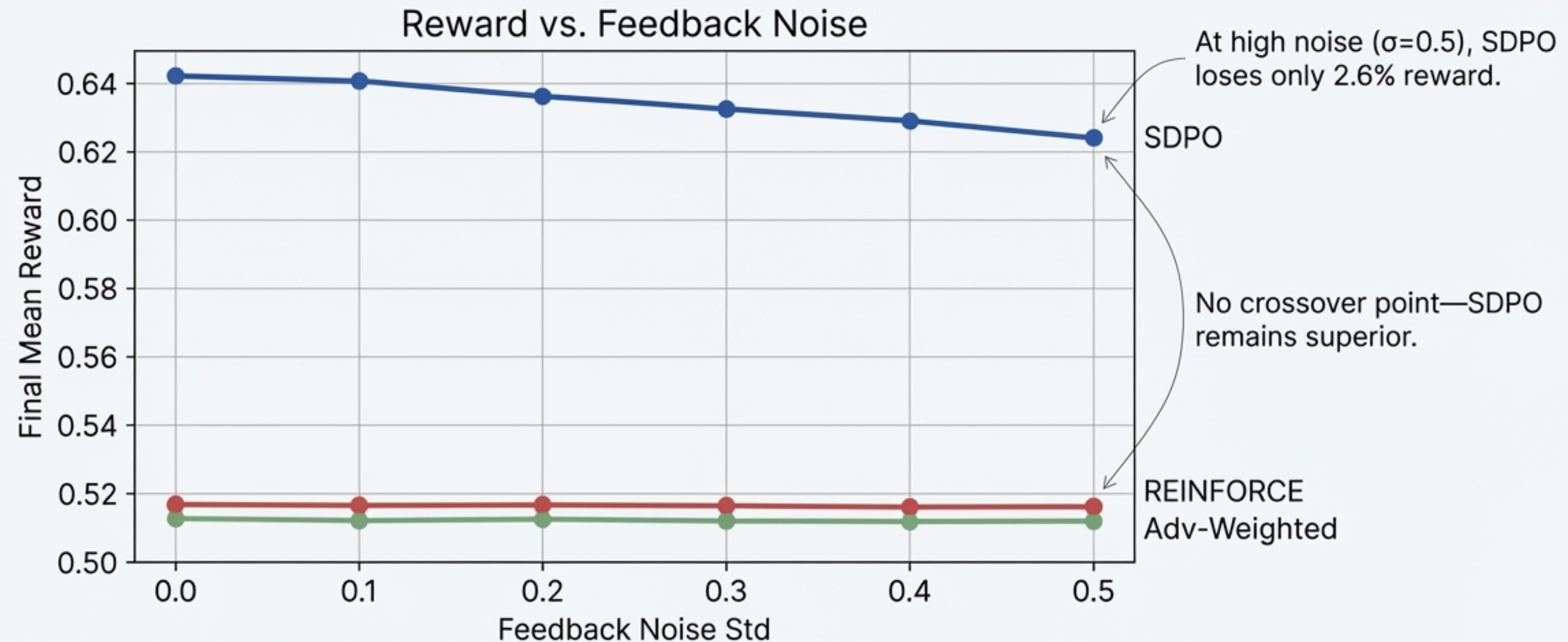


# Alignment quality scales monotonically with feedback richness.

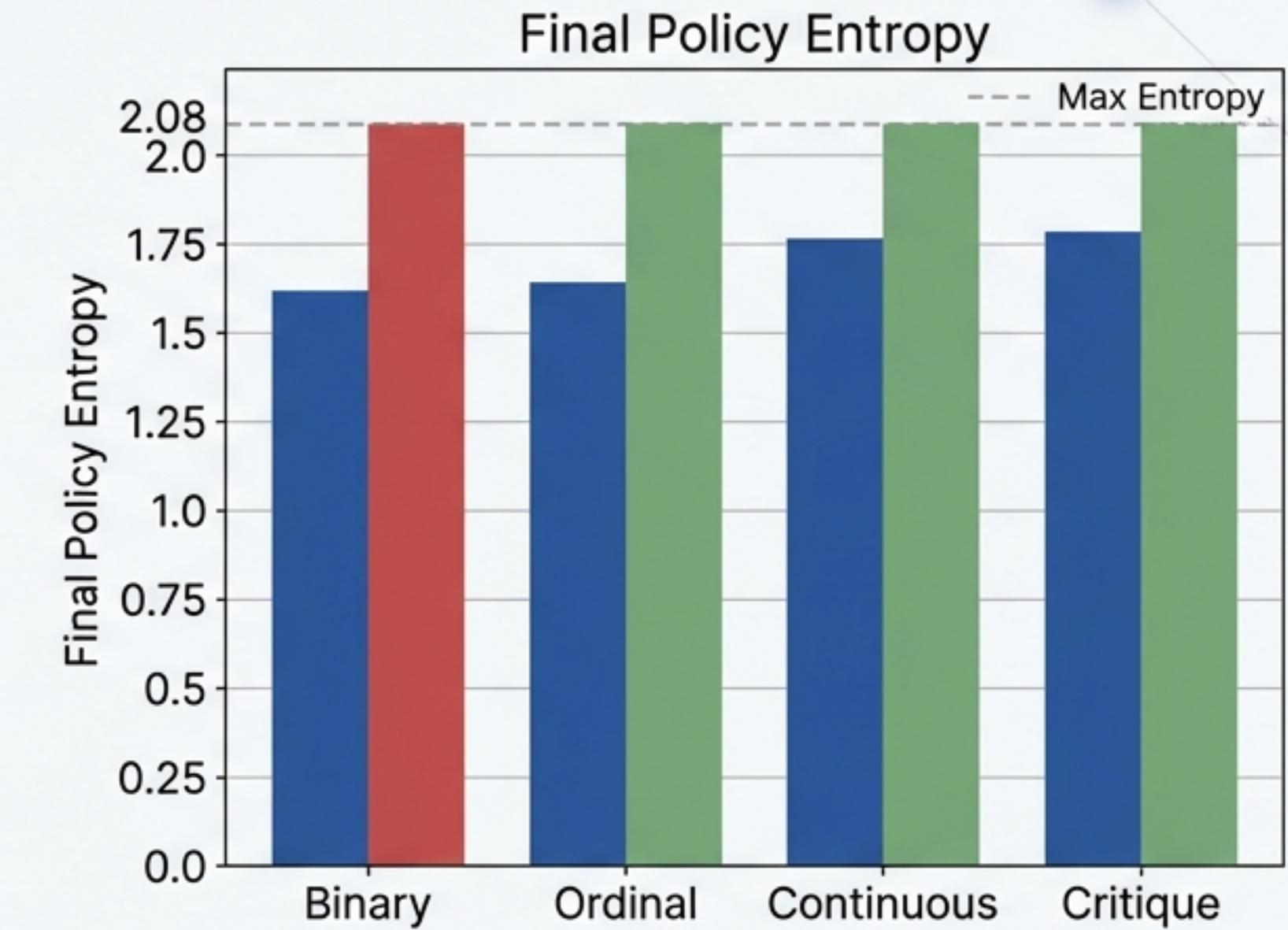
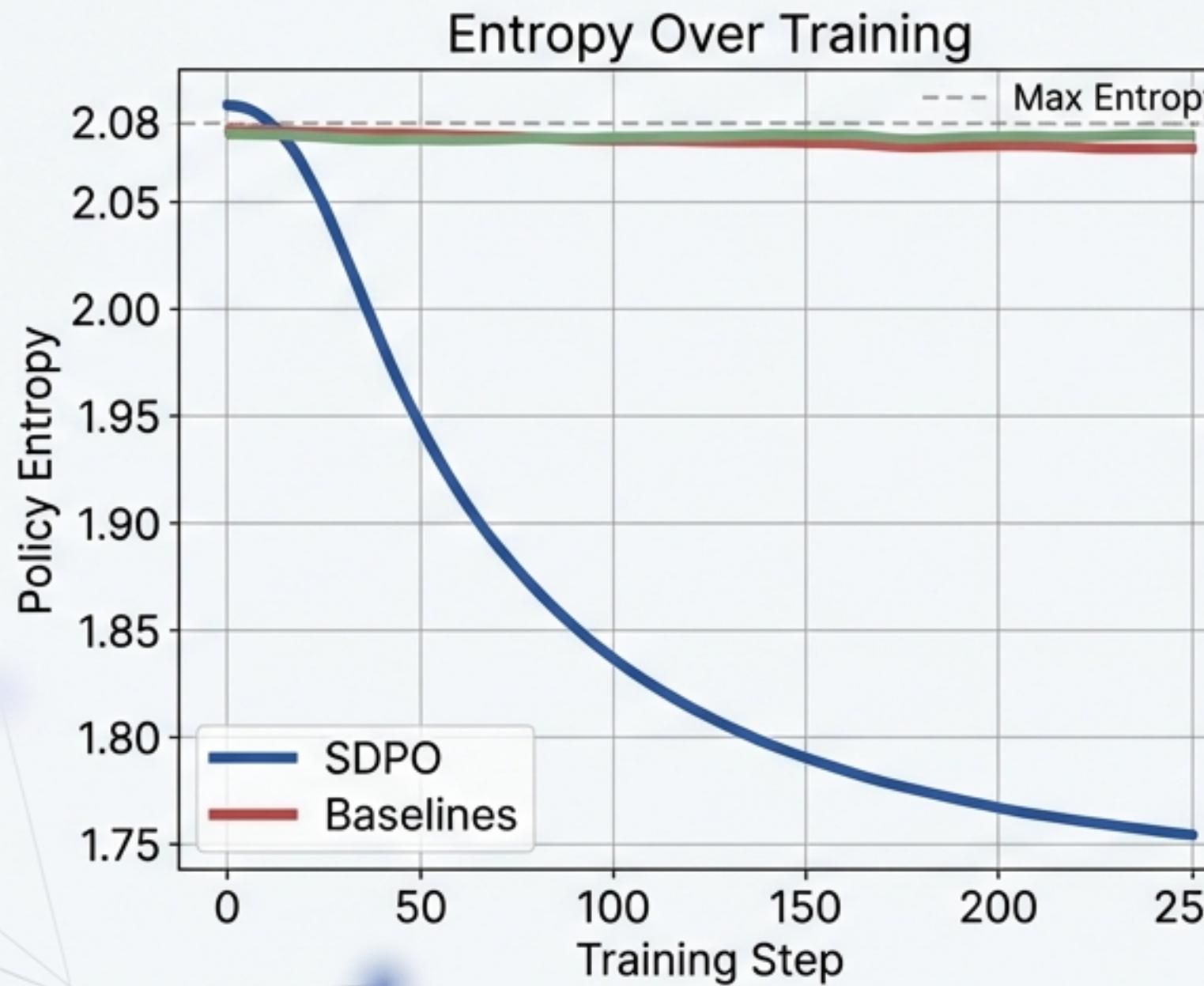


The self-teacher effectively leverages the nuanced hints in textual critique, confirming SDPO works without ground-truth verification.

# SDPO exhibits graceful degradation even under high feedback noise.



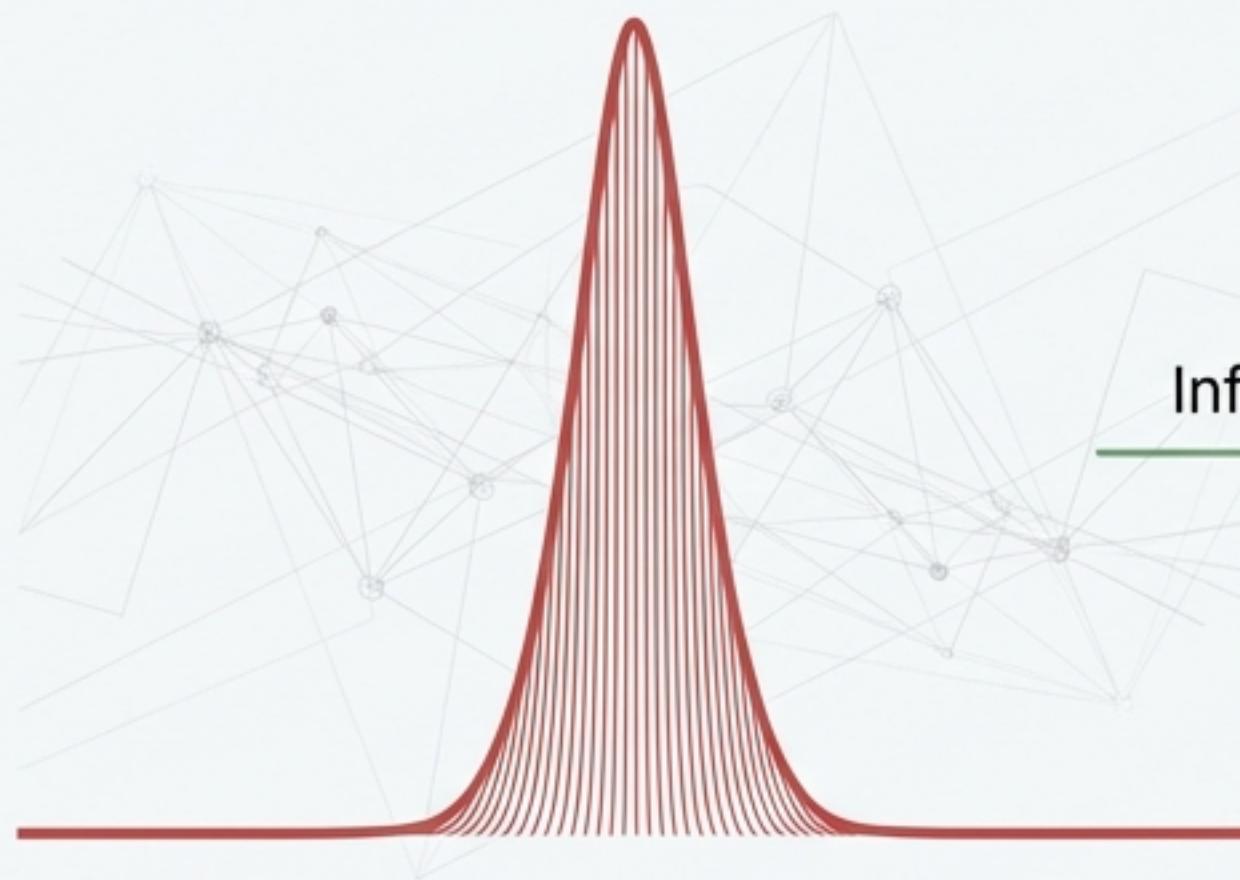
# The hidden cost of alignment is a significant reduction in diversity.



SDPO reduces policy entropy by 15–22%, risking mode collapse

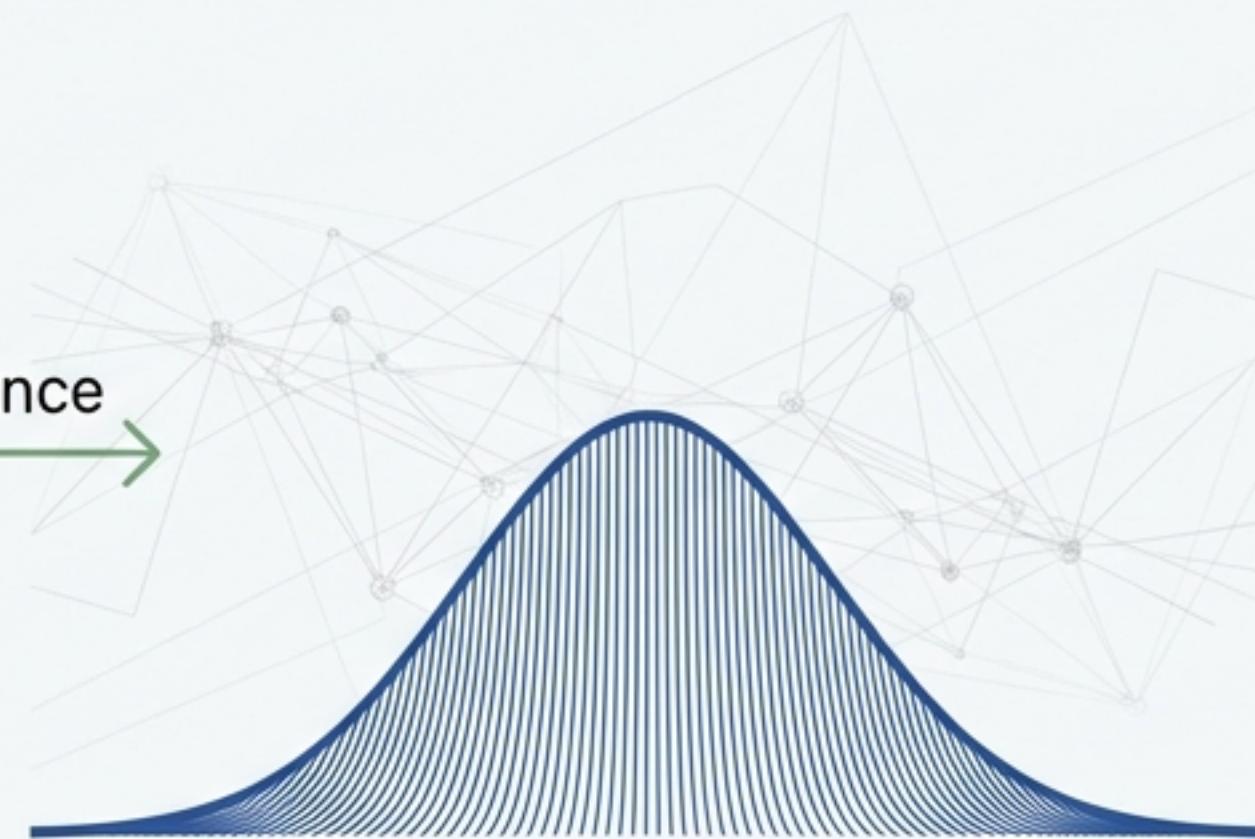
# Sharp feedback creates narrow models; nuanced critique preserves breadth.

**Binary Feedback Impact**



High Entropy Loss (22%).  
“All or nothing” signals force the teacher  
to be overly confident.

**Critique Feedback Impact**



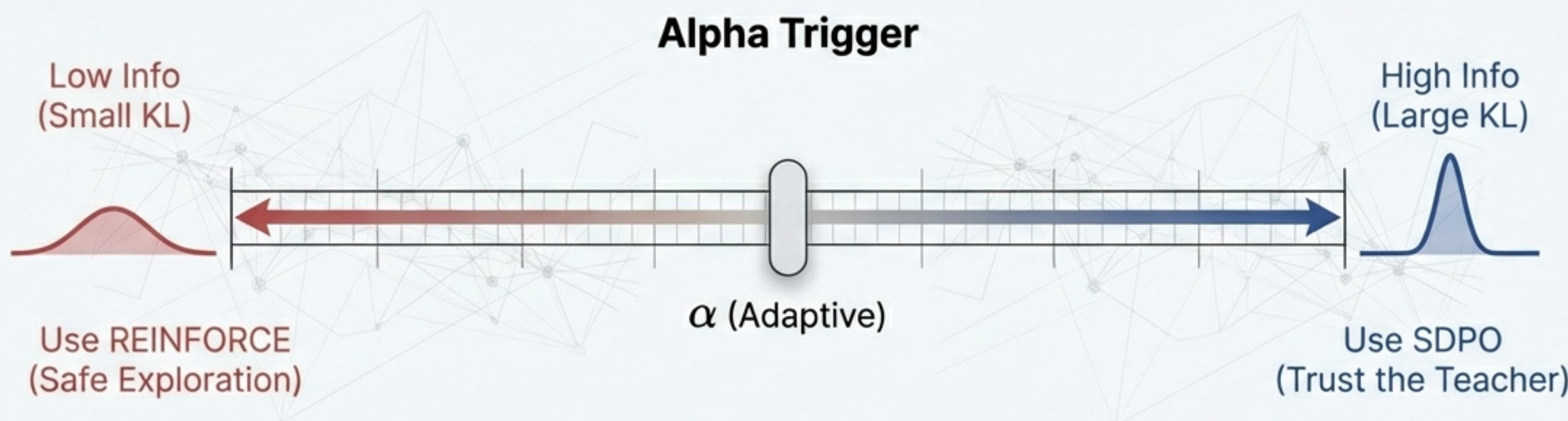
Lower Entropy Loss (14%).  
Per-token hints create a smoother, more  
complex teacher distribution.

Informational Nuance →

# The Solution: Adaptive Hybridization based on Teacher-Student divergence.

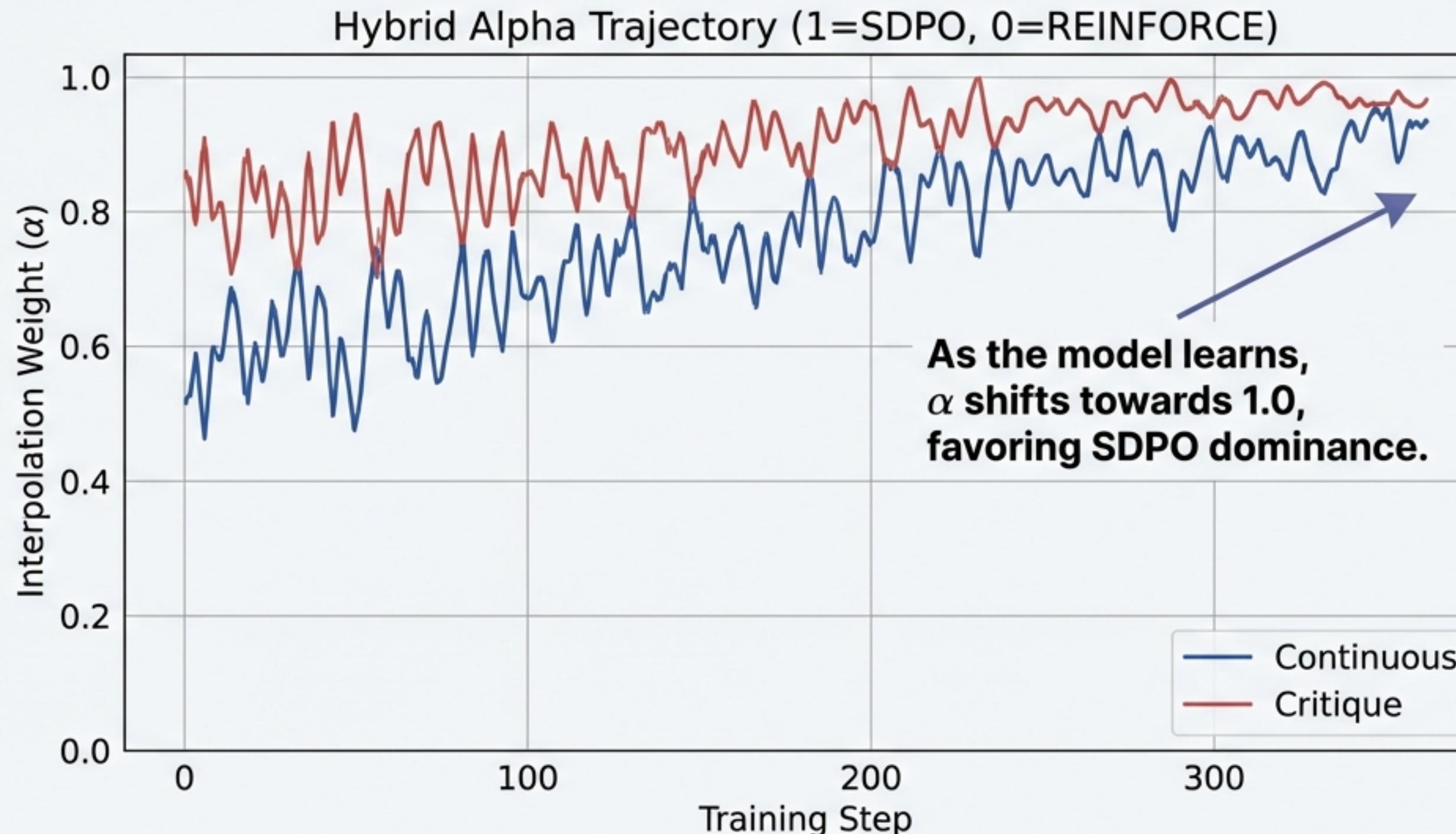
## Hybrid Formula

$$\nabla L_{hybrid} = \alpha \cdot \nabla L_{SDPO} + (1 - \alpha) \cdot \nabla L_{RF}$$



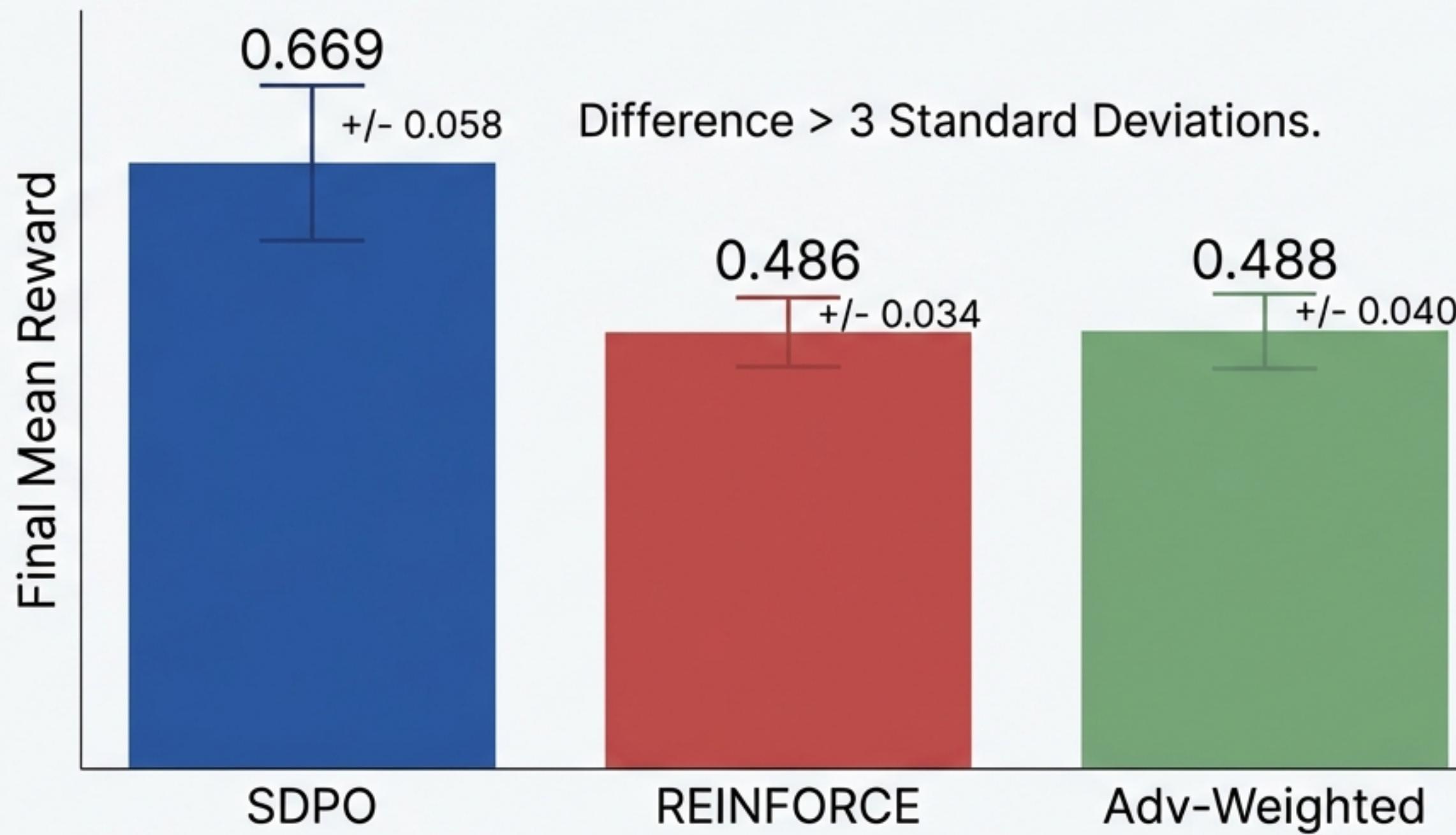
We mix Dense (SDPO) and Sparse (REINFORCE) signals dynamically during training.

# The Hybrid method adapts autonomously, shifting from exploration to alignment.



Result: Hybrid matches SDPO performance but with better entropy (1.82 vs 1.75).

# Results are statistically robust across multiple random seeds.



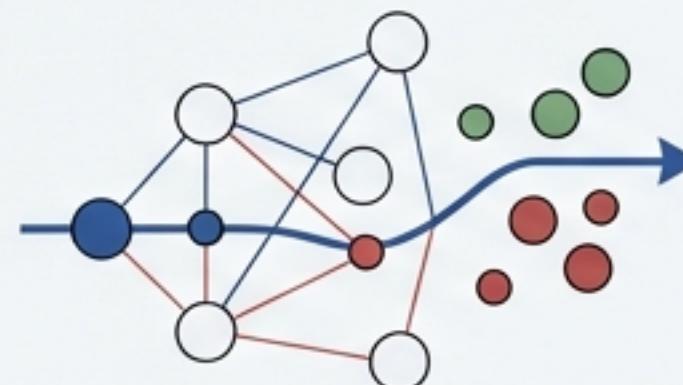
Higher variance in SDPO reflects its ability to exploit favorable reward landscapes.

**Summary: Dense signals drive better alignment, even when the destination is open-ended.**

# 1 Efficacy

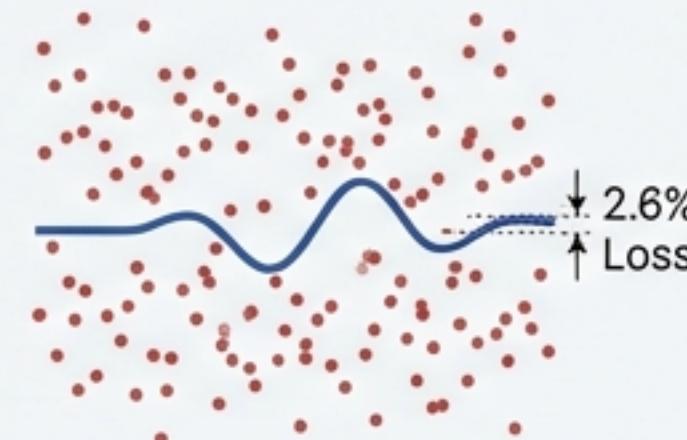
SDPO works continuous &

SDPO works for continuous & subjective rewards. It is not limited to code.



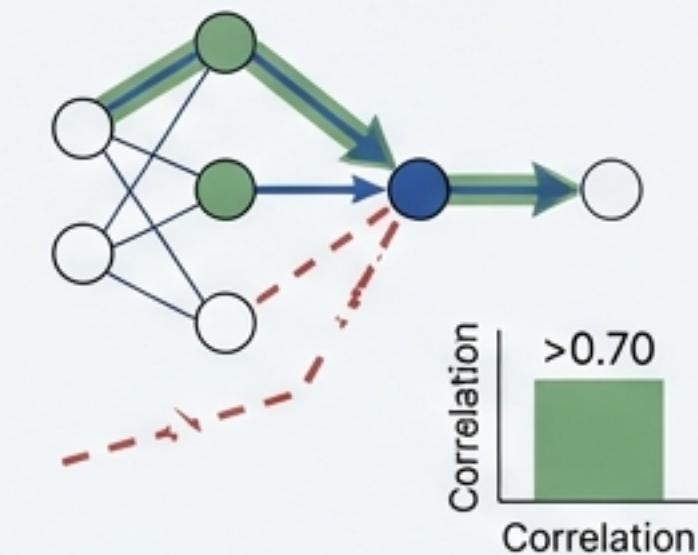
# 3 Robustness

Immune to  
evaluator noise.  
Only **2.6% loss** at  
extreme noise levels



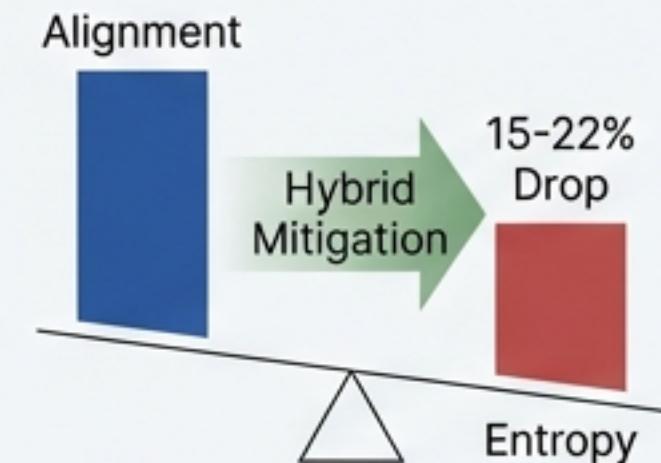
# 2 Mechanism Solves the Credit Assignment

Solves the Credit Assignment Bottleneck.  
( $>0.70$  correlation with truth).



# 4 Constraints

Diversity Trade-off.  
**15-22% entropy drop** requires Hybrid mitigation.



# Implications for deployment in real-world LLMs

## Actionable Advice



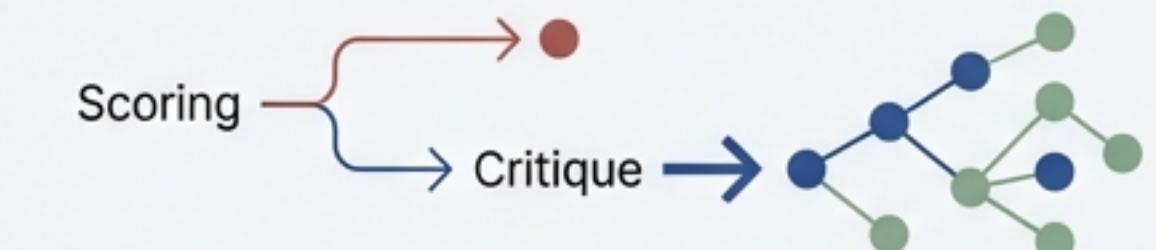
### Target Subjective Tasks

Use SDPO for post-training alignment in summarization and dialogue where ground truth is absent.



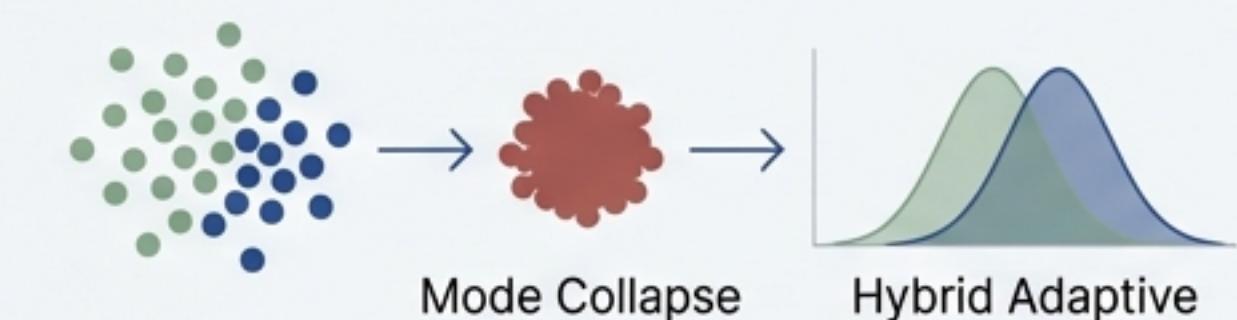
### Prioritize Critique

Invest in 'Critique' style feedback over simple scoring to preserve model diversity.



### Monitor Entropy

Watch for mode collapse. If repetitive, switch to the Hybrid Adaptive Method.

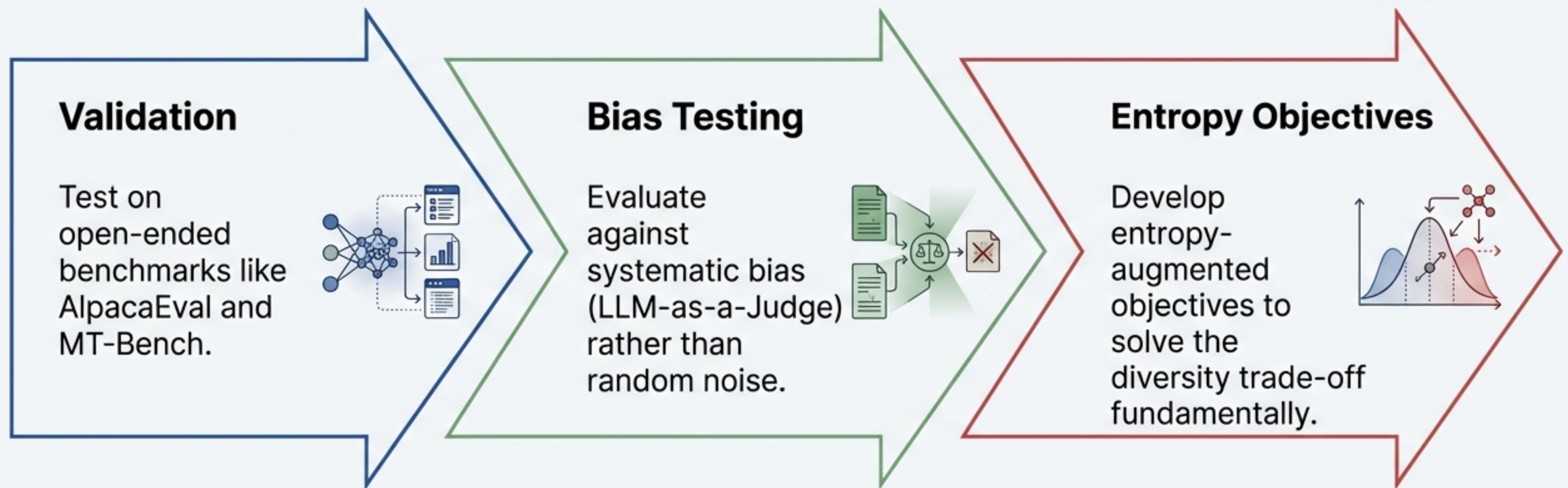


### Simplify Pipeline

SDPO removes the need for a separate Reward Model training step.



# The path forward: Scaling dense alignment to full-scale LLMs



**SDPO bridges the gap between the verifiable precision of code and the creative ambiguity of language.**